

# Mathematics

## REVISION and MODEL QUESTIONS

I. Four alternatives are given for each of the following questions/incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its alphabet in the space provided against each questions.

9) Find the LCM of the following integers by applying the prime factorization method.

17, 23 and 29

- a) 1
- b) 420
- c) 320
- d) 824

Ans:- b) 420

**Solution:**

17, 23 and 29

$$17 = 17$$

$$23 = 23$$

$$29 = 29$$

Therefore,

$$\text{LCM} = (12, 15, 21)$$

$$= 22 \times 3 \times 5 \times 7$$

$$= 420$$

10)

$(\sec^2 A - 1)$  is equal to

(A) $\tan^2 A$	(B) $\cot^2 A$
(C) $\sin^2 A$	(D) $\operatorname{cosec}^2 A$

Ans:- (A)  $\tan^2 A$

11) If the perimeter and the area of a circle are numerically equal, then the radius of the circle is

(a) 2 units	(b) $\pi$ units
(c) 4 units	(d) 7 units

Ans:- (A) 2 units

**Solution:**

Since the perimeter of the circle = area of the circle,

$$2\pi r = \pi r^2$$

$$\text{Or, } r = 2$$

So, option (A) is correct i.e. the radius of the circle is 2 units.

12)

$7 \times 11 \times 13 + 13$  is a

(A) Prime number	(B) Composite number
(C) Irrational number	(D) Odd number

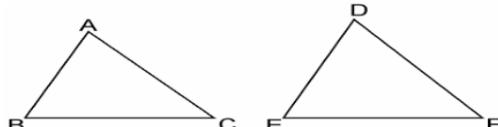
Ans:- (B) Composite number

13) Sides of two similar triangles are in the ratio 4 : 9. Areas of these triangles are in the ratio

(a) 2 : 3	(b) 4 : 9
(c) 81 : 16	(d) 16 : 81

Ans:- (D) 16 : 81

**Solution:** Given, Sides of two similar triangles are in the ratio 4 : 9.



Let ABC and DEF are two similar triangles, such that,

$$\Delta ABC \sim \Delta DEF$$

$$\text{And } AB/DE = AC/DF = BC/EF = 4/9$$

As, the ratio of the areas of these triangles will be equal to the square of the ratio of the corresponding sides,

$$\therefore \text{Area}(\Delta ABC)/\text{Area}(\Delta DEF) = AB^2/DE^2$$

$$\therefore \text{Area}(\Delta ABC)/\text{Area}(\Delta DEF) = (4/9)^2 = 16/81 = 16:81$$

Hence, the correct answer is (D).

**II. Answer the following**

1) The radii of two circles are 19 cm and 9 cm respectively. Find the radius of the circle which has a circumference equal to the sum of the circumferences of the two circles.

**Solution:**

The radius of the 1<sup>st</sup> circle = 19 cm (given)

$$\therefore \text{Circumference of the 1}^{\text{st}} \text{ circle} = 2\pi \times 19 = 38\pi \text{ cm}$$

The radius of the 2<sup>nd</sup> circle = 9 cm (given)

$$\therefore \text{Circumference of the 2}^{\text{nd}} \text{ circle} = 2\pi \times 9 = 18\pi \text{ cm}$$

So,

The sum of the circumference of two circles =

$$= 38\pi + 18\pi$$

$$= 56\pi \text{ cm}$$

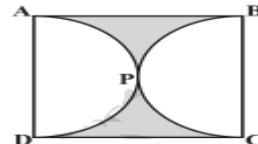
Now, let the radius of the 3<sup>rd</sup> circle = R

$$\therefore \text{The circumference of the 3}^{\text{rd}} \text{ circle} = 2\pi R$$

It is given that sum of the circumference of two circles = circumference of the 3<sup>rd</sup> circle

Hence,  $56\pi = 2\pi R$  Or, R = 28 cm.

2) Find the area of the shaded region in Fig. if ABCD is a square of side 14 cm and APD and BPC are semicircles.



**Solution:** Side of the square ABCD (as given) = 14 cm

$$\text{So, Area of ABCD} = a^2$$

$$= 14 \times 14 \text{ cm}^2 = 196 \text{ cm}^2$$

We know that the side of the square = diameter of the circle = 14 cm

So,

side of the square = diameter of the semicircle = 14 cm

$\therefore$  Radius of the semicircle = 7 cm

$$\text{Now, area of the semicircle} = (\pi R^2)/2$$

$$= (22/7 \times 7 \times 7)/2 \text{ cm}^2$$

$$= 77 \text{ cm}^2$$

$$\therefore \text{Area of two semicircles} = 2 \times 77 \text{ cm}^2 = 154 \text{ cm}^2$$

$$\text{Hence, area of the shaded region} = \text{Area of the Square} - \text{Area of two semicircles} = 196 \text{ cm}^2 - 154 \text{ cm}^2$$

$$= 42 \text{ cm}^2$$