

MATHEMATICS Chapter-5

Arithmetic Progression

To find nth term of an A.P

EXERCISE 5.2

3. In the following APs, find the missing terms in the boxes :

(i) 2, \square , 26

(ii) \square , 13, \square 3

(iii) 5, \square , \square , 91/2

(iv) -4, \square , \square , \square , \square , 6

(v) \square , 38, \square \square \square 22

Soln:

(ii) (.....Contd)

$$= 18 + 2(-5)$$

$$= 18 - 10 = 8$$

$$\text{So, Second term} = 2 + d = 2 + 12 = 14$$

Hence, the missing term in the boxes

are 18 and 8

(iii) Let the common difference of the given AP be d

$$a = 5 \quad 4\text{th term} = 9\frac{1}{2}$$

$$\Rightarrow 5 + (4-1)d = \frac{19}{2} \quad (\because a_n = a + (n-1)d)$$

$$\Rightarrow 3d = \frac{19}{2} - 5$$

$$\Rightarrow 3d = \frac{9}{2}$$

$$d = \frac{3}{2}$$

$$\therefore 2\text{nd term} = 5 + \frac{3}{2} = \frac{13}{2} = 6\frac{1}{2}$$

$$\text{and Third term} = \frac{13}{2} + \frac{3}{2} = 8$$

Hence, the missing term in the boxes

are $6\frac{1}{2}$ and 8

(iv) Let the common difference of the given AP be d

$$a = -4 \quad 6\text{th term} = 6$$

$$\Rightarrow -4 + (6-1)d = 6 \quad (\because a_n = a + (n-1)d)$$

$$\Rightarrow -4 + 5d = 6$$

$$\Rightarrow 5d = 6 + 4$$

$$\Rightarrow 5d = 10$$

$$\Rightarrow d = \frac{10}{5} \Rightarrow d = 2$$

$$\therefore 2\text{nd term} = -4 + 2 = -2$$

$$3\text{rd term} = -2 + 2 = 0$$

$$4\text{th term} = 0 + 2 = 2$$

$$5\text{th term} = 2 + 2 = 4$$

Hence, the missing term in the boxes

are -2, 0, 2, 4

(v) Let the 1st term and common difference of the given AP be a and d respectively

Then,

$$2\text{nd term} = 38$$

$$a + (2-1)d = 38 \quad (\because a_n = a + (n-1)d)$$

$$a + d = 38 \dots\dots\dots (1)$$

$$6\text{th term} = 22$$

$$a + (6-1)d = 22$$

$$a + 5d = 22 \dots\dots\dots (2)$$

Solving (1) and (2), we get

$$a = 53 \quad d = -15$$

$$\therefore 3\text{rd term} = 53 + (3-1)(-15) \quad (\because a_n = a + (n-1)d)$$

$$= 53 - 30 = 23$$

$$4\text{th term} = 53 + (4-1)(-15) \quad (\because a_n = a + (n-1)d)$$

$$= 8$$

$$5\text{th term} = 53 + (5-1)(-15) \quad (\because a_n = a + (n-1)d)$$

$$= 7$$

Hence, the missing term in the boxes

are 53, 23, 8, -7

4. Which term of the AP : 3, 8, 13, 18, ... is 78?

Soln:- The given AP is 3, 8, 13, 18, ...

$$\text{Here } a=3 \quad d=8-3=5$$

Let the nth term of the AP be 78

$$\text{Then } a_n = a + (n-1)d$$

$$78 = 3 + (n-1)(5)$$

$$5(n-1) = 78 - 3$$

$$5(n-1) = 75$$

$$n-1 = \frac{75}{5}$$

$$n-1 = 15$$

$$n = 15 + 1$$

$$n = 16$$

Hence 16th term of the AP is 78

5. Find the number of terms in each of the following APs :

(i) 7, 13, 19, ..., 205

(ii) $18, 15\frac{1}{2}, 13, \dots - 47$

Soln:- (i) 7, 13, 19, ..., 205

$$\text{Here } a = 7 \quad d = 13 - 7 = 6 \quad a_n = 205$$

Let the number of term be n

$$\text{then } a_n = 205$$

$$a + (n-1)d = 250$$

$$7 + (n-1)6 = 250$$

$$6(n-1) = 250 - 7$$

$$6(n-1) = 198$$

$$n-1 = \frac{198}{6}$$

$$n-1 = 33$$

$$n = 33 + 1 = 34$$

Hence the number of term of the given AP is 34

(Contd.....)