

MATHEMATICS Chapter-5

Arithmetic Progression

To find nth term of an A.P

EXERCISE 5.2

1. Fill in the blanks in the following table, given that a is the first term, d the common difference and a_n the n th term of the AP:

	a	d	n	a_n
(i)	7	3	8
(ii)	-18	10	0
(iii)	-3	18	-5
(iv)	-18.9	2.5	3.6
(v)	3.5	0	105

Soln : (.....Contd)

$$\begin{aligned} \text{(i)} \quad a_n &= a + (n-1)d \\ &= 7 + (8-1)3 \\ &= 7 + (7)3 \\ &= 7 + 21 \\ a_n &= 28 \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad a_n &= a + (n-1)d \\ 0 &= -18 + (10-1)d \\ 18 &= 9d \\ d &= \frac{18}{9} = 2 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad a_n &= a + (n-1)d \\ -5 &= a + (18-1)(-3) \\ -5 &= a - 51 \\ a &= 51 - 5 \\ a &= 46 \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad a_n &= a + (n-1)d \\ 3.6 &= -18.9 + (n-1)2.5 \\ 3.6 + 18.9 &= (n-1)(2.5) \\ 22.5 &= (n-1)(2.5) \\ n-1 &= \frac{22.5}{2.5} \\ &= n-1 = 9 \\ n-1 &= 9+1 \\ n &= 10 \end{aligned}$$

$$\begin{aligned} \text{(v)} \quad a_n &= a + (n-1)d \\ &= 3.5 + (105-1)0 \\ a_n &= 3.5 \end{aligned}$$

	a	d	n	a_n
(i)	7	3	8	28
(ii)	-18	2	10	0
(iii)	46	-3	18	-5
(iv)	-18.9	2.5	10	3.6
(v)	3.5	0	105	3.5

2. Choose the correct choice in the following and justify :

(i) 30th term of the AP: 10, 7, 4, ..., is

- (A) 97 (B) 77
(C) -77 (D) -87

- (ii) 11th term of the AP: $-3, -\frac{1}{2}, 2, \dots$ is
(A) 28 (B) 22
(C) -38 (D) $-48\frac{1}{2}$

Soln:- (i) The given AP is 10, 7, 4,
Here $a=10$ $D=7-10=-3$ $n=30$
we have $a_n = a + (n-1)d$

$$\begin{aligned} \text{So, } a_{30} &= 10 + (30-1)(-3) \\ &= 10 - 87 \\ a_{30} &= -77 \end{aligned}$$

Hence, the correct choice is (c) -77

- (ii) The given AP is $-3, -\frac{1}{2}, 2, \dots$

Here $a=-3$ $n=11$

$$d = -\frac{1}{2} - (-3) = -\frac{1}{2} + 3 = \frac{5}{2}$$

we have $a_n = a + (n-1)d$

$$\begin{aligned} \text{So, } a_{11} &= -3 + (11-1)\left(\frac{5}{2}\right) \\ &= -2 + 25 = 22 \end{aligned}$$

Hence, the correct choice is (B) 22

3. In the following APs, find the missing terms in the boxes :

- (i) 2, , 26
(ii) , 13, 3
(iii) 5, , , 91/2
(iv) -4, , , , 6
(v) , 38, 22

Soln:

(i) Let the common difference of the given AP be d

Then,

$$\text{Third term} = 2 + d + d = 2 + 2d$$

According to the question

$$2 + 2d = 26$$

$$2d = 26 - 2$$

$$2d = 24 \Rightarrow d = 24/2 = 12$$

$$\text{So, Second term} = 2 + d = 2 + 12 = 14$$

Hence, the missing term in the box is 14

(ii) Let the 1st term and common difference of the given AP be a and d respectively

Then,

$$\text{2nd term} = 13$$

$$a + d = 13 \dots \dots \dots (1)$$

$$\text{4th term} = 3$$

$$a + (4-1)d = 3$$

$$a + 3d = 3 \dots \dots \dots (2)$$

Solving (1) and (2), we get

$$a = 18 \quad d = -5$$

$$\therefore \text{3rd term} = a + (3-1)d$$

$$= a + 2d$$

(Contd.....)